



# Discriminative Invariant Kernel Features:

## A Bells-and-Whistles-Free Approach to Unsupervised Face Recognition and Pose Estimation

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### The Problem

**Two complementary tasks:** To perform two complementary tasks **simultaneously** using a **single unsupervised** feature extractor.

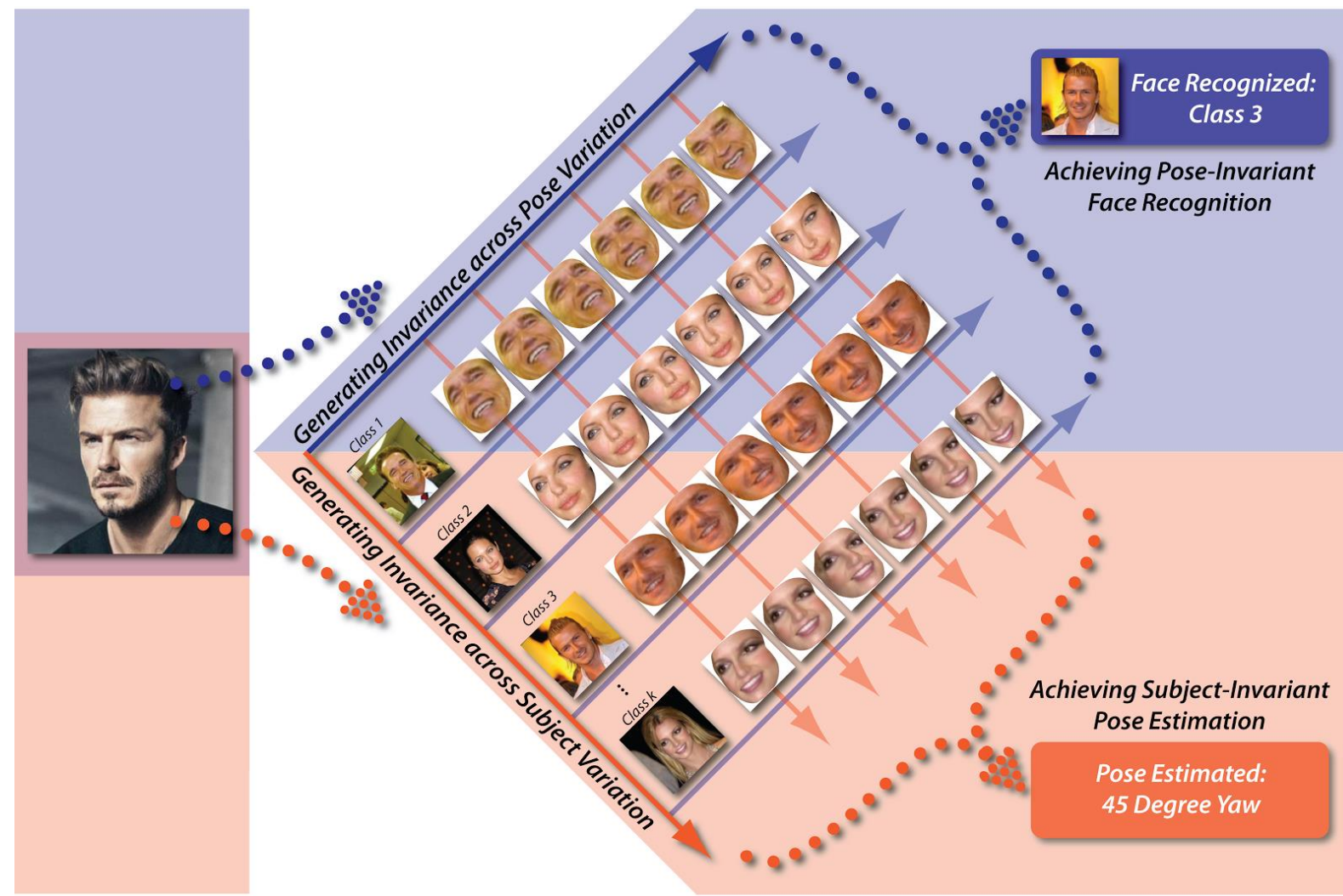


Who is this subject?

What is the subject's pose?

**Landmark-free:** The paper focuses on **dense landmark-free** (only two eye center locations) face recognition and pose estimation.

**Also extends to a completely landmark-free** approach which is also **alignment free**.



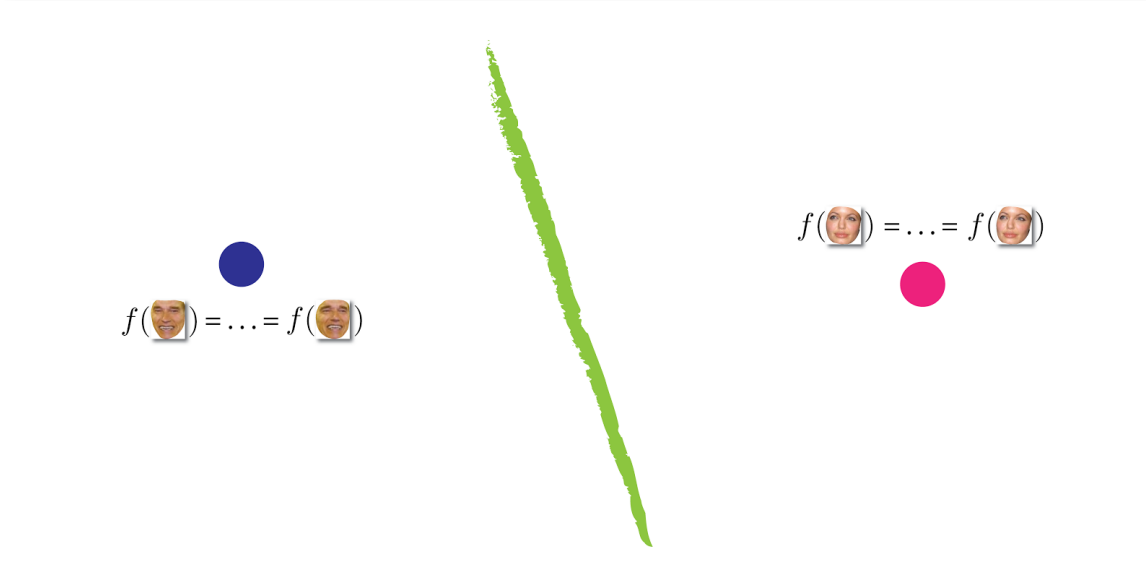
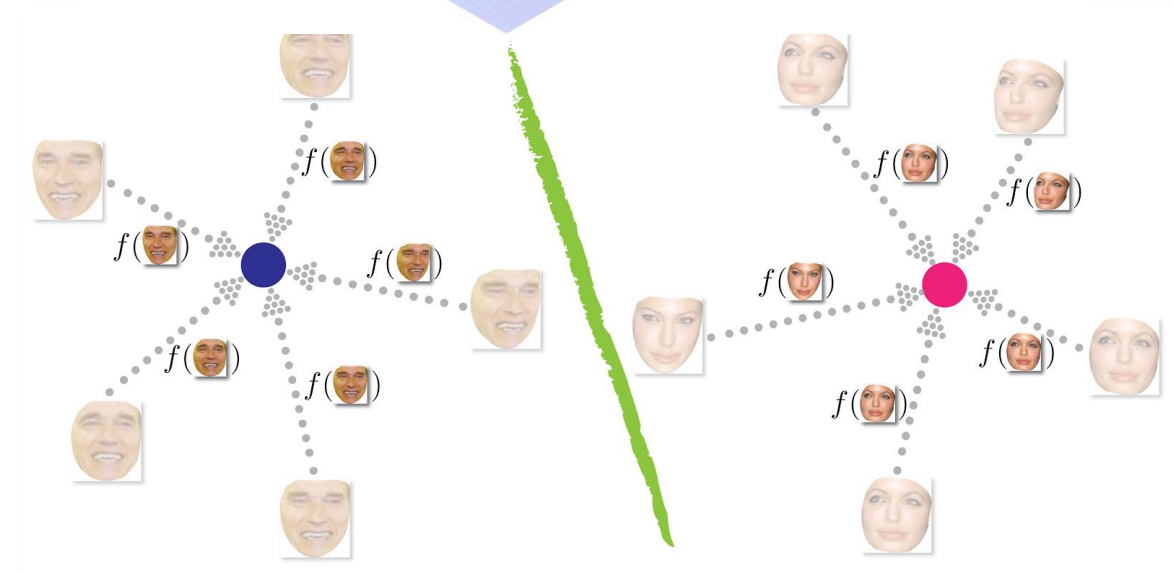
Face recognition  
sub-feature

Pose estimation  
sub-feature

### The Approach

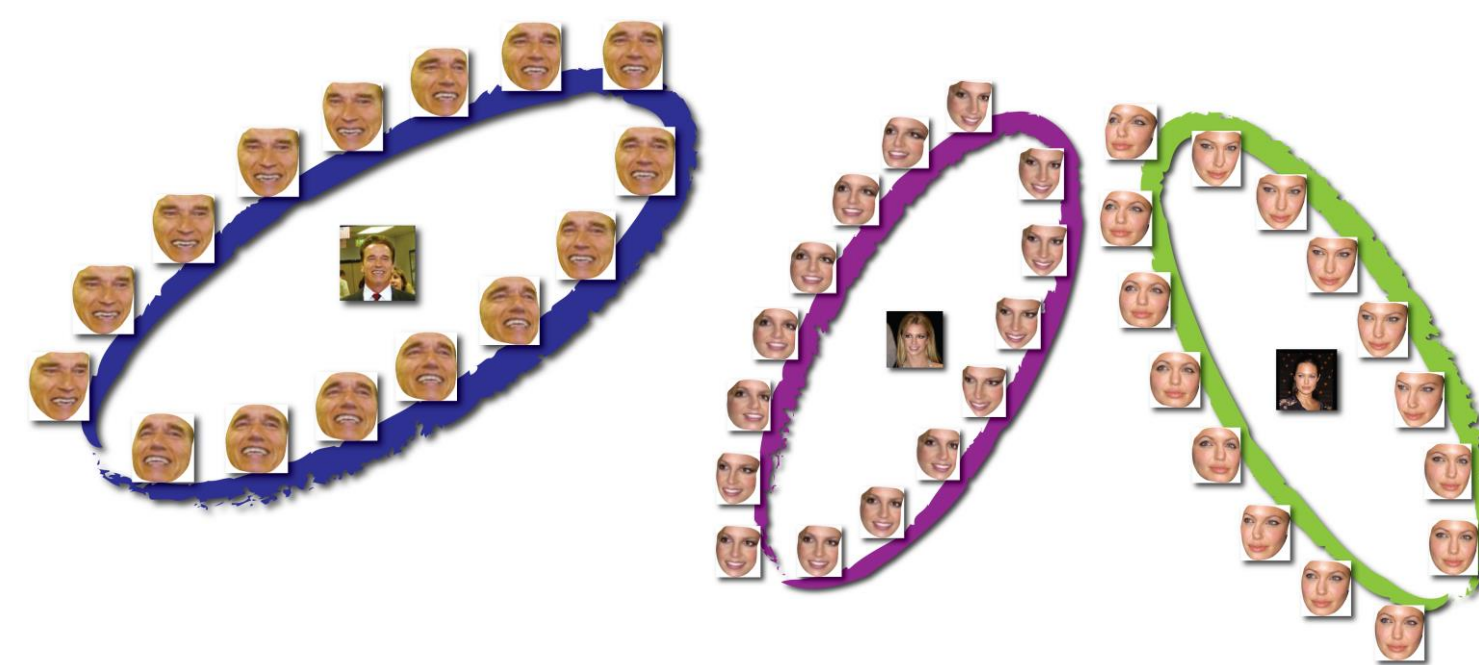
**Discriminative Invariant Feature:** We extract a **single** highly **discriminative** provably **group invariant non-linear** feature for both tasks from raw pixels.

**Invariance to Transformations:** Nuisance transformations groups such as the translation, rotation group, **increase complexity** of the learning problem. **Invariance** to such transformations can drastically **reduce complexity**.

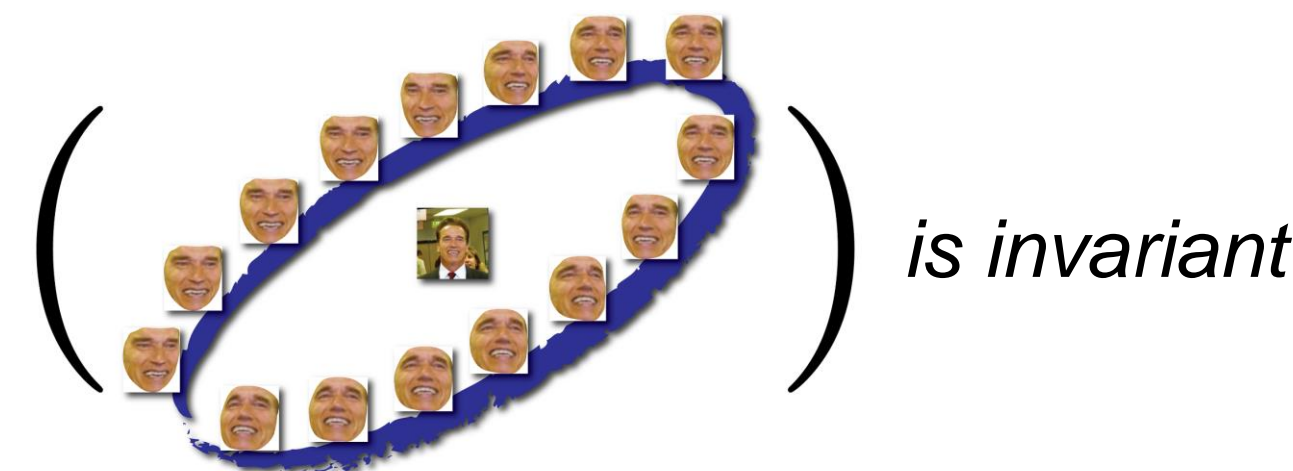


### The Approach

**Linear Invariant Features:** Previous work [1] builds linear invariant that are **implicitly** (but not explicitly) discriminative. When a group of transformations act on an object, they create an **orbit**.



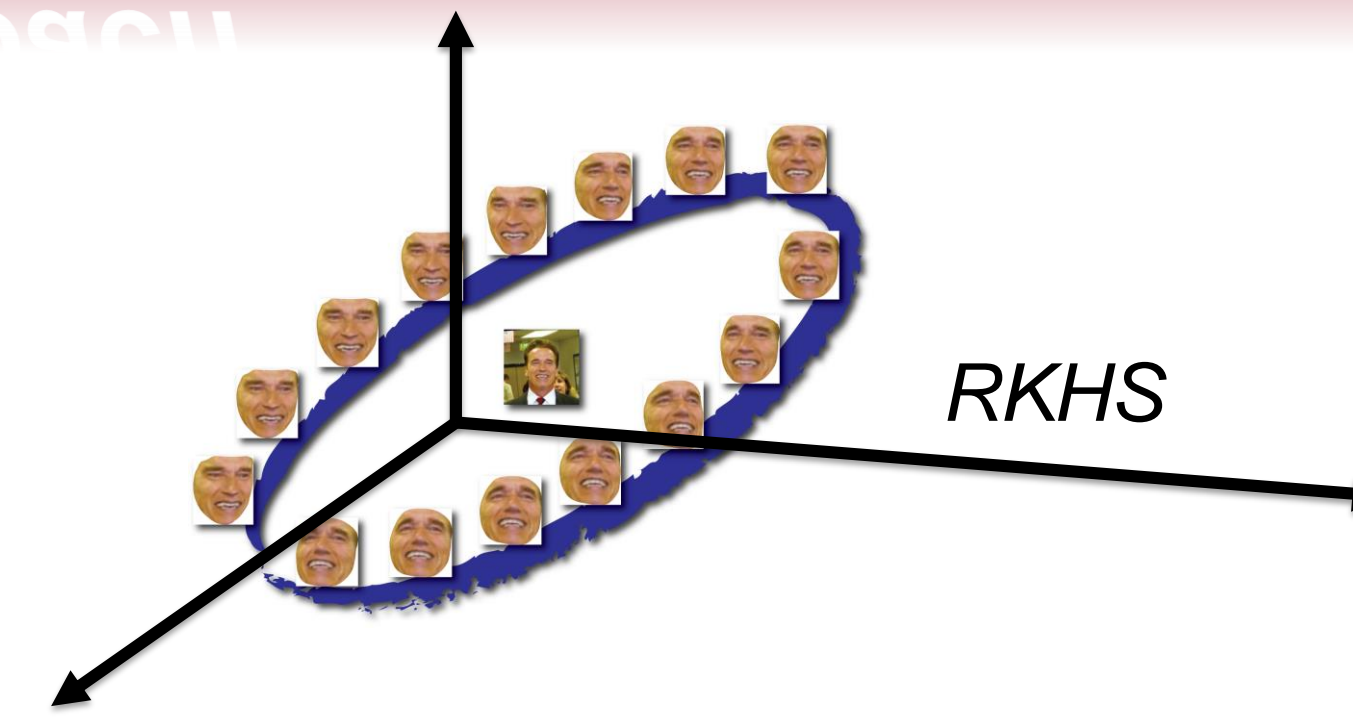
The orbit is **unique** to the object, and is an **invariant** to the transformation group



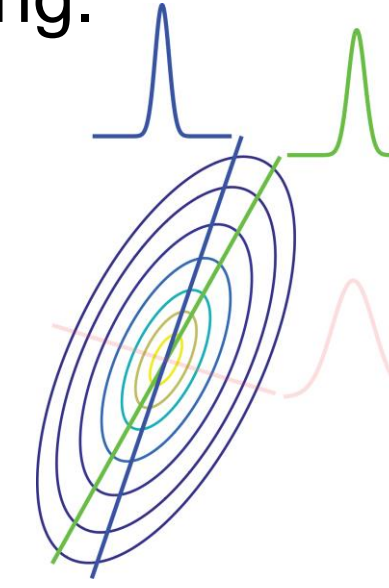
Hence **any measure** of the orbit is an **invariant implicitly discriminative** feature.



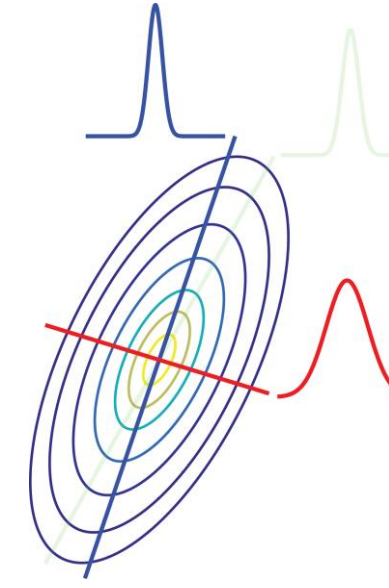
**Non-linear Discriminative Invariance:** To improve discrimination, we can compute invariant features in the RKHS. We show the **discriminative non-linear** templates form a **group** in the RKHS, leading to Discriminative Invariant Kernel Features.



To characterize the orbit, previously simply sampled templates were used. **Explicit** discrimination provides better matching.



Sampled  
templates



Discriminatively  
learned templates

The **learnt templates** still form a **group** of transformed templates, hence invariance theory holds.

**Definition 3.1 (Unitary Kernel).** We define a kernel  $k(x, y) = \langle \phi(x), \phi(y) \rangle$  to be a unitary kernel if, for a unitary group  $G$ , the mapping  $\phi(x) : \mathcal{X} \rightarrow \mathbb{H}$  satisfies  $\langle \phi(gx), \phi(gy) \rangle = \langle \phi(x), \phi(y) \rangle \forall g \in G, \forall x, y \in \mathcal{X}$ .

**Theorem 3.2** (DIKF filters form a set of transformed templates in the kernel space under a group). *Given a group  $G$  of unitary transformation elements  $g$  with  $|G| = N$ , if  $k(x, y) = \langle \phi(x), \phi(y) \rangle$  i.e.  $k$  is a unitary kernel, and  $\{\mathbf{X}_n \mid \mathbf{X}_n = g_n(\mathbf{X}), g_n \in G\}$  are a set of pre-whitened matrices acted upon by  $G$ , then the set of DIKF filters*

$$\mathcal{T}_k = \left\{ \Phi(\mathbf{t}_{kn}) = \Phi(\mathbf{X}_n) (\Phi(\mathbf{X}_n) \cdot \Phi(\mathbf{X}_n))^{-1} \mathbf{u}_k \mid \forall n \right\}$$

is a set of transformed templates under a group.

### The Experiments

(1) **Face recognition (153,000 semi-synthetic image dataset):** 1000 subjects with 153 poses each. Images rendered from a 3D model with real texture. We compare DIKF against sampled templates (NDP) and discriminative linear templates (DILF).

(2) **Face recognition (LFW):** Max-pooled DIKF (in **red**) matches state-of-the-art results on two LFW protocols, despite being simpler than competing methods and working on raw pixels.

(3) **Pose estimation:** 15 poses (-40 to 40 yaw and -20 to 20 pitch, step of 20). Train on the 250 subjects and test on the 1500 images of the remaining 100 subjects.

